

Polinomios, geometría, aplicaciones, Matemax... y mucho mas!

Carlos D'Andrea

Universitat de Barcelona



Conferencia en honor a.....

Conferencia en honor a.....



Q ∞ Crear una cuenta Acceder ...

Alicia Dickenstein

15 Idiomas

Artículo [Discusión](#)

Leer [Editar](#) [Ver historial](#) [Herramientas](#)

Alicia Marcela Dickenstein (17 de enero de 1955, ciudad de [Buenos Aires](#)) es una [matemática](#), [investigadora](#) y [profesora argentina](#) conocida por su trabajo en [geometría algebraica](#), particularmente geometría teórica.

Biografía [\[editar \]](#)

Egresó en 1972 del bachillerato del [Colegio Nacional de Buenos Aires](#).¹ En 1973 comenzó a estudiar la [licenciatura](#) en Ciencias Matemáticas en la [Facultad de Ciencias Exactas y Naturales de la Universidad de Buenos Aires](#), recibéndose en 1977.² En 1982, obtuvo el título de [Doctora](#) en Ciencias Matemáticas en la misma institución, bajo la dirección de Miguel Herrera³, con una tesis sobre geometría analítica compleja.

Fue la primera directora del Departamento de Matemática de la Facultad de Ciencias Exactas y Naturales de la UBA (en el período 1996-1998), donde desde 2009 pasó a ser profesora regular titular plenaria.⁴

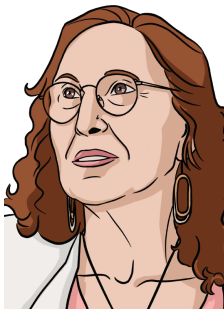
Alicia Dickenstein



Información personal

Carlos D'Andrea

Polinomios, geometría, aplicaciones, Matemax.... y mucho mas!



Alicia Dickenstein (b. 1955)

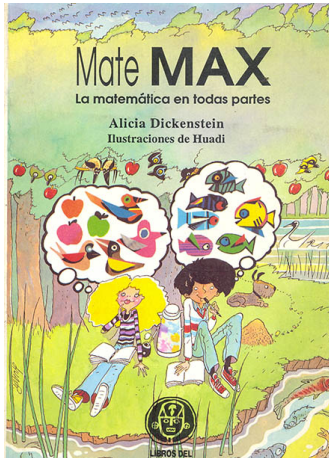
Alicia Dickenstein was born in Buenos Aires, Argentina. She completed her BS in mathematics in 1977 and her PhD in 1982 at the University of Buenos Aires, where she is now a full professor. Dickenstein's research is in algebraic geometry and its applications. She has published over 80 research papers and supervised 7 graduate and 20 undergraduate students. Dickenstein is a Fellow of the AMS (2019) and SIAM (2020) and received the 2021 L'Oréal-UNESCO International Award for Women in Science. She also served as a vice-president of the International Mathematical Union (IMU). In addition to her research, Dickenstein co-authored *Matemax*, a problem-solving book for children presented in both Spanish and English.

This poster is part of the EvenQuads project, which combines innovative mathematical card games with learning about amazing women mathematicians. The project celebrates the 50th anniversary of the Association for Women in Mathematics.

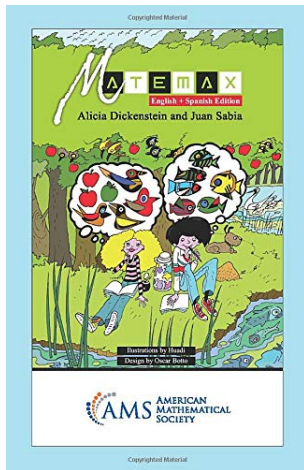
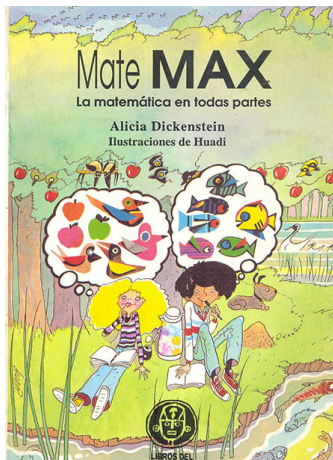


MateMax

MateMax



MateMax



Un problema del MateMax

Un problema del MateMax

Torneo eliminatorio



64 jugadoras van a competir en un torneo de tenis. En cada partido, la jugadora que pierda quedará eliminada, pero le regalarán un par de zapatillas marca “Gabriela Corazón”. La que gane un partido, volverá a jugar contra otra rival, hasta que se determine la ganadora del torneo.

¿Cuántos pares de zapatillas van a regalar ?

¿Cuántos partidos van a jugarse en total para hallar la ganadora ?



Conferencia Científica

Conferencia Científica

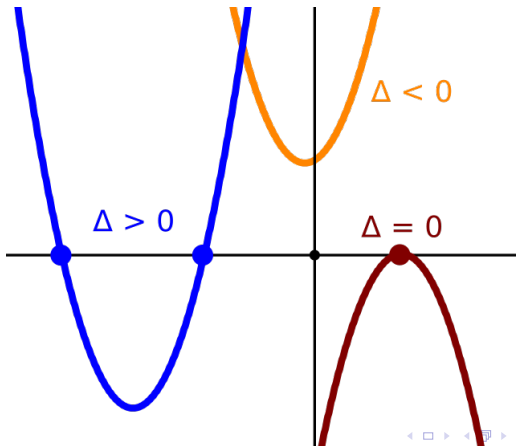
Publications (by number in area)

Algebraic geometry Biology and other natural sciences Classical thermodynamics, heat transfer Combinatorics
Commutative rings and algebras Computer science Convex and discrete geometry General History and biography Numerical analysis Several complex variables and analytic spaces
Special functions

Una que sepamos tod@s

Una que sepamos tod@s

DISCRIMINANTES



Discriminante de una cuadrática

Discriminante de una cuadrática

$ax^2 + bx + c$ tiene discriminante
 $\Delta = b^2 - 4ac$

Discriminante de una cuadrática

$ax^2 + bx + c$ tiene discriminante

$$\Delta = b^2 - 4ac$$

$$x = \frac{-b \pm \sqrt{b^2 - 4ac}}{2a}$$

Discriminant

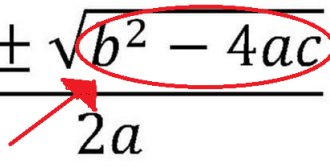
Discriminante de una cuadrática

$ax^2 + bx + c$ tiene discriminante

$$\Delta = b^2 - 4ac$$

$$x = \frac{-b \pm \sqrt{b^2 - 4ac}}{2a}$$

Discriminant

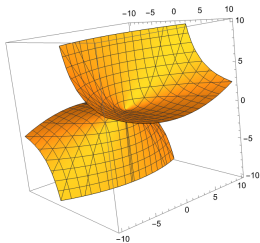


$\Delta = 0 \iff$ la cuadrática tiene una
única raíz

Geometría del discriminante

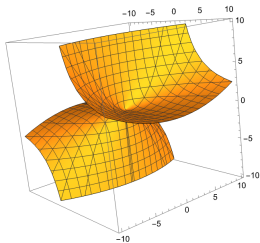
Geometría del discriminante

En el espacio (a, b, c) la ecuación $b^2 - 4ac = 0$ define una superficie



Geometría del discriminante

En el espacio (a, b, c) la ecuación $b^2 - 4ac = 0$ define una superficie



racional: $(u, v) \mapsto (u^2, 2uv, v^2)$



Discriminante de la cúbica

Discriminante de la cúbica

$$ax^3 + bx^2 + cx + d$$

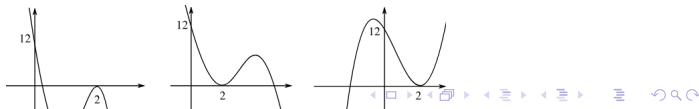
Discriminante de la cúbica

$$\begin{aligned} & ax^3 + bx^2 + cx + d \\ \Delta = & -27a^2d^2 + 18abcd - 4ac^3 \\ & -4b^3d + b^2c^2 \end{aligned}$$

Discriminante de la cúbica

$$ax^3 + bx^2 + cx + d$$
$$\Delta = -27a^2d^2 + 18abcd - 4ac^3 - 4b^3d + b^2c^2$$

se anula cuando hay una raíz doble +

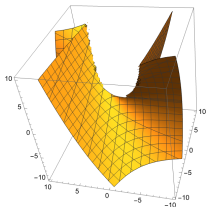


Geometría



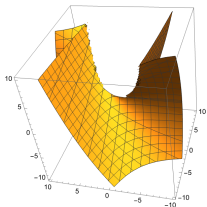
Geometría

$$-27a^2d^2 + 18abcd - 4ac^3 - 4b^3d + b^2c^2 = 0$$



Geometría

$$-27a^2d^2 + 18abcd - 4ac^3 - 4b^3d + b^2c^2 = 0$$



Superficie racional:

$$(u, v, w) \mapsto (w^3, -2uw^2 - vw^2, u^2w + 2uvw, -u^2v)$$



En general...

En general...

$$f(x) = a_n x^n + a_{n-1} x^{n-1} + \dots + a_1 x + a_0$$

existe $\Delta \in \mathbb{Z}[a_0, a_1, \dots, a_n]$

En general...

$$f(x) = a_n x^n + a_{n-1} x^{n-1} + \dots + a_1 x + a_0$$

existe $\Delta \in \mathbb{Z}[a_0, a_1, \dots, a_n]$ que se anula cuando $f(x)$ no tiene n raíces (complejas) distintas

En general...

$$f(x) = a_n x^n + a_{n-1} x^{n-1} + \dots + a_1 x + a_0$$

existe $\Delta \in \mathbb{Z}[a_0, a_1, \dots, a_n]$ que se anula cuando $f(x)$ no tiene n raíces (complejas) distintas

$$\Delta = 0 \subset \mathbb{C}^{n+1}$$

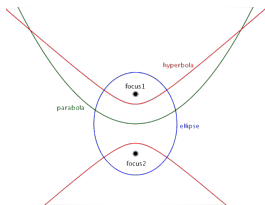
es una (hiper) superficie racional

Generalizaciones?

Generalizaciones?

Mas variables

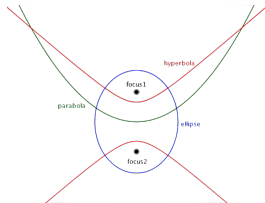
$$a + bx + cy + dx^2 + ey^2 + fxy$$



Generalizaciones?

Mas variables

$$a + bx + cy + dx^2 + ey^2 + fxy$$

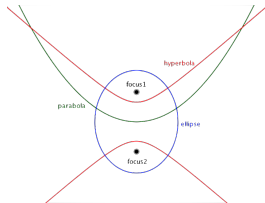


$$\Delta = -4adf + ae^2 + b^2f - bce + c^2d$$

Generalizaciones?

Mas variables

$$a + bx + cy + dx^2 + ey^2 + fxy$$



$$\Delta = -4adf + ae^2 + b^2f - bce + c^2d$$

se anula si hay un punto **singular**



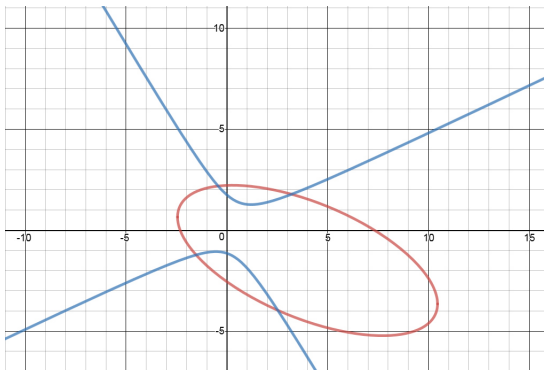
Otra generalización

Otra generalización

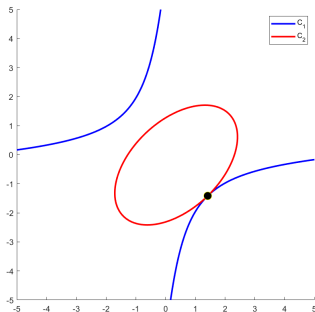
$$a + bx + cy + dx^2 + fxy + dy^2$$
$$a' + b'x + c'y + d'x^2 + f'xy + dy^2$$

Otra generalización

$$a + bx + cy + dx^2 + fxy + dy^2$$
$$a' + b'x + c'y + d'x^2 + f'xy + dy^2$$



El discriminante



Detecta intersecciones singulares

¿Quién es?

¿Quién es?

$\Delta =$

¿Quién es?

$$\begin{aligned} \Delta = & 16(a')^2(d')^4d^6 + (a')^2(f')^4d^6 + 16a'(b')^2(d')^3d^6 - 2a'b'c'(f')^3d^6 + 4(b')^4(d')^2d^6 + \\ & 4(b')^2(c')^2(d')^2d^6 + (b')^2(c')^2(f')^2d^6 + 8(a')^2(d')^2(f')^2d^6 - 4a'(b')^2d'(f')^2d^6 - \\ & 8a'b'c'(d')^2f'd^6 + 4(b')^3c'd'f'd^6 - 32aa'(d')^5d^5 - 16a(b')^2(d')^4d^5 + 16a(c')^2(d')^4d^5 - \\ & 48ba'b'(d')^4d^5 - 16ca'c'(d')^4d^5 - 6aa'd'(f')^4d^5 - 24b(b')^3(d')^3d^5 - 8bb'(c')^2(d')^3d^5 - \\ & 16c(b')^2c'(d')^3d^5 + 8fa'b'c'(d')^3d^5 - 4f(a')^2d'(f')^3d^5 + 6ca'b'd'(f')^3d^5 + 2ba'c'd'(f')^3d^5 + \\ & 6ab'c'd'(f')^3d^5 - 8f(b')^3c'(d')^2d^5 - 32aa'(d')^3(f')^2d^5 + 12a(b')^2(d')^2(f')^2d^5 + \\ & 4a(c')^2(d')^2(f')^2d^5 + 4ba'b'(d')^2(f')^2d^5 - 4ca'c'(d')^2(f')^2d^5 - 2bb'(c')^2d'(f')^2d^5 - \\ & 6c(b')^2c'd'(f')^2d^5 + 6fa'b'c'd'(f')^2d^5 - 16f(a')^2(d')^3f'd^5 - 8ca'b'(d')^3f'd^5 + \\ & 8ba'c'(d')^3f'd^5 + 40ab'c'(d')^3f'd^5 - 12c(b')^3(d')^2f'd^5 + 16fa'(b')^2(d')^2f'd^5 - \\ & 12b(b')^2c'(d')^2f'd^5 - 2f(b')^2(c')^2d'f'd^5 + 16a^2(d')^6d^4 + 32b^2a'(d')^5d^4 + 16c^2a'(d')^5d^4 + \\ & 48abb'(d')^5d^4 - 16acc'(d')^5d^4 + 52b^2(b')^2(d')^4d^4 + 12c^2(b')^2(d')^4d^4 + 16cfa'b'(d')^4d^4 + \\ & 40bc'b'c'(d')^4d^4 - 56afb'c'(d')^4d^4 + 9a^2(d')^2(f')^4d^4 + b^2a'd'(f')^4d^4 + 20cf(b')^3(d')^3d^4 - \\ & 20f^2a'(b')^2(d')^3d^4 + 28bf(b')^2c'(d')^3d^4 - 4bca'(d')^2(f')^3d^4 + 28afa'(d')^2(f')^3d^4 - \\ & 18acb'(d')^2(f')^3d^4 - 10abc'(d')^2(f')^3d^4 - 2bfa'b'd'(f')^3d^4 - b^2b'c'd'(f')^3d^4 - \\ & f^2(b')^4(d')^2d^4 + 24a^2(d')^4(f')^2d^4 + 4b^2a'(d')^3(f')^2d^4 + 12c^2a'(d')^3(f')^2d^4 - \\ & 28abb'(d')^3(f')^2d^4 - 12acc'(d')^3(f')^2d^4 + 4f^2(a')^2(d')^2(f')^2d^4 - b^2(b')^2(d')^2(f')^2d^4 + \\ & 9c^2(b')^2(d')^2(f')^2d^4 - 24cfa'b'(d')^2(f')^2d^4 - 4bfa'c'(d')^2(f')^2d^4 + 14bc'b'c'(d')^2(f')^2d^4 - \\ & 18afb'c'(d')^2(f')^2d^4 + f^2a'(b')^2d'(f')^2d^4 + 2bf(b')^2c'd'(f')^2d^4 + 16bca'(d')^4f'd^4 + \\ & 80afa'(d')^4f'd^4 - 24acb'(d')^4f'd^4 - 56abc'(d')^4f'd^4 + 48bc(b')^2(d')^3f'd^4 - \\ & 40af(b')^2(d')^3f'd^4 - 8af(c')^2(d')^3f'd^4 - 16bfa'b'(d')^3f'd^4 + 8cfa'c'(d')^3f'd^4 \end{aligned}$$

$$\begin{aligned}
& +4b^2b'c'(d')^3f'd^4 + 2bf(b')^3(d')^2f'd^4 + 4bfb'(c')^2(d')^2f'd^4 + 14cf(b')^2c'(d')^2f'd^4 - \\
& 4f^2a'b'c'(d')^2f'd^4 - f^2(b')^3c'd'f'd^4 - 32ab^2(d')^6d^3 - 32af^2a'(d')^5d^3 - 32bcfa'(d')^5d^3 - \\
& 48b^3b'(d')^5d^3 - 32bc^2b'(d')^5d^3 + 32acfb'(d')^5d^3 - 16b^2cc'(d')^5d^3 + 64abfc'(d')^5d^3 + \\
& 40af^2(b')^2(d')^4d^3 - 80bcf(b')^2(d')^4d^3 + 32bf^2a'b'(d')^4d^3 - 24b^2fb'c'(d')^4d^3 - 2ab^2(d')^2(f')^4d^3 + \\
& 4bf^2(b')^3(d')^3d^3 - 4cf^2(b')^2c'(d')^3d^3 + 24abc(d')^3(f')^3d^3 - 48a^2f(d')^3(f')^3d^3 - \\
& 4b^2fa'(d')^2(f')^3d^3 + 2b^2cb'(d')^2(f')^3d^3 + 4abfb'(d')^2(f')^3d^3 + 2b^3c'(d')^2(f')^3d^3 + \\
& 2f^3(b')^3c'(d')^2d^3 + 16ab^2(d')^4(f')^2d^3 - 40af^2a'(d')^3(f')^2d^3 + 8bcfa'(d')^3(f')^2d^3 + \\
& 4b^3b'(d')^3(f')^2d^3 - 24bc^2b'(d')^3(f')^2d^3 + 72acfb'(d')^3(f')^2d^3 - 4b^2cc'(d')^3(f')^2d^3 + \\
& 32abfc'(d')^3(f')^2d^3 - 2af^2(b')^2(d')^2(f')^2d^3 - 4bcf(b')^2(d')^2(f')^2d^3 + 8bf^2a'b'(d')^2(f')^2d^3 - \\
& 2b^2fb'c'(d')^2(f')^2d^3 + 32abc(d')^5f'd^3 - 64a^2f(d')^5f'd^3 - 16b^2fa'(d')^4f'd^3 - 32c^2fa'(d')^4f'd^3 - \\
& 56b^2cb'(d')^4f'd^3 + 80abfb'(d')^4f'd^3 + 8b^3c'(d')^4f'd^3 + 32acfc'(d')^4f'd^3 - 8b^2f(b')^2(d')^3f'd^3 - \\
& 24c^2f(b')^2(d')^3f'd^3 + 32cf^2a'b'(d')^3f'd^3 + 8af^2b'c'(d')^3f'd^3 - 32bcfb'c'(d')^3f'd^3 + \\
& 2cf^2(b')^3(d')^2f'd^3 - 4f^3a'(b')^2(d')^2f'd^3 - 2bf^2(b')^2c'(d')^2f'd^3 + 16b^4(d')^6d^2 + 16b^2c^2(d')^6d^2 + \\
& 32a^2f^2(d')^6d^2 - 32abcf(d')^6d^2 + 16c^2f^2a'(d')^5d^2 - 80abf^2b'(d')^5d^2 + 96b^2cfb'(d')^5d^2 - \\
& 16acf^2c'(d')^5d^2 - 4b^2f^2(b')^2(d')^4d^2 + 12c^2f^2(b')^2(d')^4d^2 - 16cf^3a'b'(d')^4d^2 + 8af^3b'c'(d')^4d^2 + \\
& 8bcf^2b'c'(d')^4d^2 - 4cf^3(b')^3(d')^3d^2 + 4f^4a'(b')^2(d')^3d^2 - 4bf^3(b')^2c'(d')^3d^2 - \\
& 4b^3c(d')^3(f')^3d^2 + 8ab^2f(d')^3(f')^3d^2 - 4b^4(d')^4(f')^2d^2 + 12b^2c^2(d')^4(f')^2d^2 + \\
& 88a^2f^2(d')^4(f')^2d^2 - 88abcf(d')^4(f')^2d^2 + 4b^2f^2a'(d')^3(f')^2d^2 - 16abf^2b'(d')^3(f')^2d^2 + \\
& 4b^2cfb'(d')^3(f')^2d^2 - 4b^3fc'(d')^3(f')^2d^2 + 16b^3c(d')^5f'd^2 - 32ab^2f(d')^5f'd^2 + 16af^3a'(d')^4f'd^2 - \\
& 88acf^2b'(d')^4f'd^2 + 8b^3fb'(d')^4f'd^2 + 64bc^2fb'(d')^4f'd^2 - 24abf^2c'(d')^4f'd^2 + 8b^2cfc'(d')^4f'd^2 + \\
& 8af^3(b')^2(d')^3f'd^2 + 4bcf^2(b')^2(d')^3f'd^2 - 8bf^3a'b'(d')^3f'd^2 + 8b^2f^2b'c'(d')^3f'd^2 + \\
& 32ab^2f^2(d')^6d - 32b^3cf(d')^6d + 32acf^3b'(d')^5d - 32bc^2f^2b'(d')^5d - 8af^4(b')^2(d')^4d
\end{aligned}$$

$$\begin{aligned} &+8bcf^3 (b')^2 (d')^4 d - 8ab^2f^2 (d')^4 (f')^2 d + 8b^3cf (d')^4 (f')^2 d - 64a^2f^3 (d')^5 f' d + \\ &96abcf^2 (d')^5 f' d - 32b^2c^2f (d')^5 f' d + 16abf^3b' (d')^4 f' d - 16b^2cf^2b' (d')^4 f' d + 16a^2f^4 (d')^6 - \\ &32abcf^3 (d')^6 + 16b^2c^2f^2 (d')^6 \end{aligned}$$



Una generalizacion más

Una generalización más

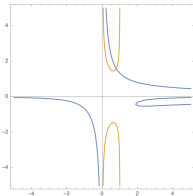
$$a + bx^2y + cx^3y^3$$

Una generalización más

$$a + bx^2y + cx^3y^3$$
$$a' + b'xy^2 + c'x^4y^2$$

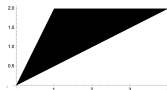
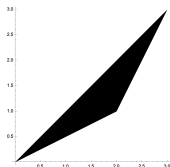
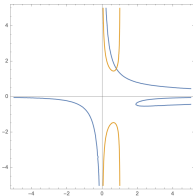
Una generalización más

$$a + bx^2y + cx^3y^3$$
$$a' + b'xy^2 + c'x^4y^2$$



Una generalización más

$$a + bx^2y + cx^3y^3$$
$$a' + b'xy^2 + c'x^4y^2$$



¿Quién es Δ ?

¿Quién es Δ ?

$$\begin{aligned} & 1024a^2 (a')^9 c^{20} + 4096a^4 (a')^6 (b')^2 c^{19} + 3072a^2 b (a')^8 b' c^{19} + 4096a^6 (a')^3 (b')^4 c^{18} + \\ & 6144a^2 b^2 (a')^7 (b')^2 c^{18} + 6144a^4 (a')^6 (b')^2 c' c^{18} + 6144a^2 b (a')^8 b' c' c^{18} - 12288a^6 b (a')^2 (b')^5 c^{17} - \\ & 24576a^4 b^2 (a')^4 (b')^4 c^{17} - 2048a^2 b^3 (a')^6 (b')^3 c^{17} + 3072a^4 (a')^6 (b')^2 (c')^2 c^{17} + \\ & 12288a^6 (a')^3 (b')^4 c' c^{17} + 12288a^4 b (a')^5 (b')^3 c' c^{17} + 18432a^2 b^2 (a')^7 (b')^2 c' c^{17} + \\ & 12288a^6 b^2 a' (b')^6 c^{16} + 32768a^4 b^3 (a')^3 (b')^5 c^{16} - 9216a^2 b^4 (a')^5 (b')^4 c^{16} + 512a^4 (a')^6 (b')^2 (c')^3 c^{16} + \\ & 15360a^6 (a')^3 (b')^4 (c')^2 c^{16} + 18432a^4 b (a')^5 (b')^3 (c')^2 c^{16} + 16896a^2 b^2 (a')^7 (b')^2 (c')^2 c^{16} - \\ & 36864a^6 b (a')^2 (b')^5 c' c^{16} - 61440a^4 b^2 (a')^4 (b')^4 c' c^{16} + 18432a^2 b^3 (a')^6 (b')^3 c' c^{16} - \\ & 4096a^6 b^3 (b')^7 c^{15} - 6144a^4 b^4 (a')^2 (b')^6 c^{15} - 15360a^2 b^5 (a')^4 (b')^5 c^{15} + 10240a^6 (a')^3 (b')^4 (c')^3 c^{15} + \\ & 9216a^4 b (a')^5 (b')^3 (c')^3 c^{15} - 46080a^6 b (a')^2 (b')^5 (c')^2 c^{15} - 46080a^4 b^2 (a')^4 (b')^4 (c')^2 c^{15} + \\ & 41472a^2 b^3 (a')^6 (b')^3 (c')^2 c^{15} + 36864a^6 b^2 a' (b')^6 c' c^{15} + 49152a^4 b^3 (a')^3 (b')^5 c' c^{15} - \\ & 24576a^2 b^4 (a')^5 (b')^4 c' c^{15} - 12288a^4 b^5 a' (b')^7 c^{14} + 10240a^2 b^6 (a')^3 (b')^6 c^{14} + \\ & 3840a^6 (a')^3 (b')^4 (c')^4 c^{14} + 1536a^4 b (a')^5 (b')^3 (c')^4 c^{14} - 30720a^6 b (a')^2 (b')^5 (c')^3 c^{14} - \\ & 7680a^4 b^2 (a')^4 (b')^4 (c')^3 c^{14} + 26624a^2 b^3 (a')^6 (b')^3 (c')^3 c^{14} + 46080a^6 b^2 a' (b')^6 (c')^2 c^{14} + \\ & 9216a^2 b^4 (a')^5 (b')^4 (c')^2 c^{14} - 12288a^6 b^3 (b')^7 c' c^{14} + 27648a^4 b^4 (a')^2 (b')^6 c' c^{14} - \\ & 61440a^2 b^5 (a')^4 (b')^5 c' c^{14} + 6144a^4 b^6 (b')^8 c^{13} + 6144a^2 b^7 (a')^2 (b')^7 c^{13} + 768a^6 (a')^3 (b')^4 (c')^5 c^{13} - \\ & 11520a^6 b (a')^2 (b')^5 (c')^4 c^{13} + 3840a^4 b^2 (a')^4 (b')^4 (c')^4 c^{13} + 30720a^6 b^2 a' (b')^6 (c')^3 c^{13} - \\ & 30720a^4 b^3 (a')^3 (b')^5 (c')^3 c^{13} + 44544a^2 b^4 (a')^5 (b')^4 (c')^3 c^{13} - 15360a^6 b^3 (b')^7 (c')^2 c^{13} + \\ & 78336a^4 b^4 (a')^2 (b')^6 (c')^2 c^{13} - 92160a^2 b^5 (a')^4 (b')^5 (c')^2 c^{13} - 55296a^4 b^5 a' (b')^7 c' c^{13} + \\ & 3072a^2 b^8 a' (b')^8 c^{12} + 64a^6 (a')^3 (b')^4 (c')^6 c^{12} - 2304a^6 b (a')^2 (b')^5 (c')^5 c^{12} + \\ & 1152a^4 b^2 (a')^4 (b')^4 (c')^5 c^{12} + 11520a^6 b^2 a' (b')^6 (c')^4 c^{12} - 15360a^4 b^3 (a')^3 (b')^5 (c')^4 c^{12} \end{aligned}$$

$$\begin{aligned}
& +25536a^2b^4 (a')^5 (b')^4 (c')^4 c^{12} - 10240a^6b^3 (b')^7 (c')^3 c^{12} + 65280a^4b^4 (a')^2 (b')^6 (c')^3 c^{12} - \\
& 38400a^2b^5 (a')^4 (b')^5 (c')^3 c^{12} - 82944a^4b^5a' (b')^7 (c')^2 c^{12} - 61440a^2b^6 (a')^3 (b')^6 (c')^2 c^{12} + \\
& 21504a^4b^6 (b')^8 c' c^{12} + 36864a^2b^7 (a')^2 (b')^7 c' c^{12} - 3072a^2b^9 (b')^9 c^{11} - 192a^6b (a')^2 (b')^5 (c')^6 c^{11} + \\
& 2304a^6b^2a' (b')^6 (c')^5 c^{11} - 1536a^4b^3 (a')^3 (b')^5 (c')^5 c^{11} - 3840a^6b^3 (b')^7 (c')^4 c^{11} + \\
& 21120a^4b^4 (a')^2 (b')^6 (c')^4 c^{11} + 18240a^2b^5 (a')^4 (b')^5 (c')^4 c^{11} - 56832a^4b^5a' (b')^7 (c')^3 c^{11} - \\
& 102400a^2b^6 (a')^3 (b')^6 (c')^3 c^{11} + 29184a^4b^6 (b')^8 (c')^2 c^{11} + 55296a^2b^7 (a')^2 (b')^7 (c')^2 c^{11} + \\
& 18432a^2b^8a' (b')^8 c' c^{11} + 192a^6b^2a' (b')^6 (c')^6 c^{10} + 256a^4b^3 (a')^3 (b')^5 (c')^6 c^{10} - \\
& 768a^6b^3 (b')^7 (c')^5 c^{10} + 1728a^4b^4 (a')^2 (b')^6 (c')^5 c^{10} + 14592a^2b^5 (a')^4 (b')^5 (c')^5 c^{10} - \\
& 19200a^4b^5a' (b')^7 (c')^4 c^{10} - 57600a^2b^6 (a')^3 (b')^6 (c')^4 c^{10} + 20224a^4b^6 (b')^8 (c')^3 c^{10} + \\
& 15360a^2b^7 (a')^2 (b')^7 (c')^3 c^{10} + 50688a^2b^8a' (b')^8 (c')^2 c^{10} - 12288a^2b^9 (b')^9 c' c^{10} + \\
& 512b^{12} (b')^{10} c^9 - 64a^6b^3 (b')^7 (c')^6 c^9 - 96a^4b^4 (a')^2 (b')^6 (c')^6 c^9 - 3456a^4b^5a' (b')^7 (c')^5 c^9 - \\
& 4224a^2b^6 (a')^3 (b')^6 (c')^5 c^9 + 8064a^4b^6 (b')^8 (c')^4 c^9 - 30720a^2b^7 (a')^2 (b')^7 (c')^4 c^9 + \\
& 69120a^2b^8a' (b')^8 (c')^3 c^9 - 19968a^2b^9 (b')^9 (c')^2 c^9 + 48a^4b^4 (a')^2 (b')^6 (c')^7 c^8 - \\
& 576a^4b^5a' (b')^7 (c')^6 c^8 + 4512a^2b^6 (a')^3 (b')^6 (c')^6 c^8 + 2112a^4b^6 (b')^8 (c')^5 c^8 - \\
& 26496a^2b^7 (a')^2 (b')^7 (c')^5 c^8 + 47040a^2b^8a' (b')^8 (c')^4 c^8 - 14848a^2b^9 (b')^9 (c')^3 c^8 + \\
& 2304b^{12} (b')^{10} c' c^8 - 96a^4b^5a' (b')^7 (c')^7 c^7 + 416a^4b^6 (b')^8 (c')^6 c^7 - 5472a^2b^7 (a')^2 (b')^7 (c')^6 c^7 + \\
& 12672a^2b^8a' (b')^8 (c')^5 c^7 - 2496a^2b^9 (b')^9 (c')^4 c^7 + 4608b^{12} (b')^{10} (c')^2 c^7 + 48a^4b^6 (b')^8 (c')^7 c^6 + \\
& 576a^2b^7 (a')^2 (b')^7 (c')^7 c^6 - 1248a^2b^8a' (b')^8 (c')^6 c^6 + 3456a^2b^9 (b')^9 (c')^5 c^6 + \\
& 5376b^{12} (b')^{10} (c')^3 c^6 - 960a^2b^8a' (b')^8 (c')^7 c^5 + 2208a^2b^9 (b')^9 (c')^6 c^5 + 4032b^{12} (b')^{10} (c')^4 c^5 + \\
& 12a^2b^8a' (b')^8 (c')^8 c^4 + 384a^2b^9 (b')^9 (c')^7 c^4 + 2016b^{12} (b')^{10} (c')^5 c^4 - 12a^2b^9 (b')^9 (c')^8 c^3 + \\
& 672b^{12} (b')^{10} (c')^6 c^3 + 144b^{12} (b')^{10} (c')^7 c^2 + 18b^{12} (b')^{10} (c')^8 c + b^{12} (b')^{10} (c')^9
\end{aligned}$$

¿Qué sabemos de Δ ?

¿Qué sabemos de Δ ?

- No necesariamente hay “un” Δ

¿Qué sabemos de Δ ?

- No necesariamente hay “un” Δ
- Homogeneidades

¿Qué sabemos de Δ ?

- No necesariamente hay “un” Δ
- Homogeneidades
- Invariencias

¿Qué sabemos de Δ ?

- No necesariamente hay “un” Δ
- Homogeneidades
- Invariencias
- $\Delta = 0$ es una hipersuperficie racional

¿Qué sabemos de Δ ?

- No necesariamente hay “un” Δ
- Homogeneidades
- Invariencias
- $\Delta = 0$ es una hipersuperficie racional
- “Se puede” calcular

Desafío

Desafío

Calcular Δ

7267	222	226	229	230	231	232	233	234	235	236	237	238	239	240	241	242	243	244	245	246	247	248	249	250	251	252	253	254	255	256	257	258	259	260	261	262	263	264	265	266	267	268	269	270	271	272	273	274	275	276	277	278	279	280	281	282	283	284	285	286	287	288	289	290	291	292	293	294	295	296	297	298	299	300	301	302	303	304	305	306	307	308	309	310	311	312	313	314	315	316	317	318	319	320	321	322	323	324	325	326	327	328	329	330	331	332	333	334	335	336	337	338	339	340	341	342	343	344	345	346	347	348	349	350	351	352	353	354	355	356	357	358	359	360	361	362	363	364	365	366	367	368	369	370	371	372	373	374	375	376	377	378	379	380	381	382	383	384	385	386	387	388	389	390	391	392	393	394	395	396	397	398	399	400	401	402	403	404	405	406	407	408	409	410	411	412	413	414	415	416	417	418	419	420	421	422	423	424	425	426	427	428	429	430	431	432	433	434	435	436	437	438	439	440	441	442	443	444	445	446	447	448	449	450	451	452	453	454	455	456	457	458	459	460	461	462	463	464	465	466	467	468	469	470	471	472	473	474	475	476	477	478	479	480	481	482	483	484	485	486	487	488	489	490	491	492	493	494	495	496	497	498	499	500	501	502	503	504	505	506	507	508	509	510	511	512	513	514	515	516	517	518	519	520	521	522	523	524	525	526	527	528	529	530	531	532	533	534	535	536	537	538	539	540	541	542	543	544	545	546	547	548	549	550	551	552	553	554	555	556	557	558	559	560	561	562	563	564	565	566	567	568	569	570	571	572	573	574	575	576	577	578	579	580	581	582	583	584	585	586	587	588	589	590	591	592	593	594	595	596	597	598	599	600	601	602	603	604	605	606	607	608	609	610	611	612	613	614	615	616	617	618	619	620	621	622	623	624	625	626	627	628	629	630	631	632	633	634	635	636	637	638	639	640	641	642	643	644	645	646	647	648	649	650	651	652	653	654	655	656	657	658	659	660	661	662	663	664	665	666	667	668	669	670	671	672	673	674	675	676	677	678	679	680	681	682	683	684	685	686	687	688	689	690	691	692	693	694	695	696	697	698	699	700	701	702	703	704	705	706	707	708	709	710	711	712	713	714	715	716	717	718	719	720	721	722	723	724	725	726	727	728	729	730	731	732	733	734	735	736	737	738	739	740	741	742	743	744	745	746	747	748	749	750	751	752	753	754	755	756	757	758	759	760	761	762	763	764	765	766	767	768	769	770	771	772	773	774	775	776	777	778	779	780	781	782	783	784	785	786	787	788	789	790	791	792	793	794	795	796	797	798	799	800	801	802	803	804	805	806	807	808	809	810	811	812	813	814	815	816	817	818	819	820	821	822	823	824	825	826	827	828	829	830	831	832	833	834	835	836	837	838	839	840	841	842	843	844	845	846	847	848	849	850	851	852	853	854	855	856	857	858	859	860	861	862	863	864	865	866	867	868	869	870	871	872	873	874	875	876	877	878	879	880	881	882	883	884	885	886	887	888	889	890	891	892	893	894	895	896	897	898	899	900	901	902	903	904	905	906	907	908	909	910	911	912	913	914	915	916	917	918	919	920	921	922	923	924	925	926	927	928	929	930	931	932	933	934	935	936	937	938	939	940	941	942	943	944	945	946	947	948	949	950	951	952	953	954	955	956	957	958	959	960	961	962	963	964	965	966	967	968	969	970	971	972	973	974	975	976	977	978	979	980	981	982	983	984	985	986	987	988	989	990	991	992	993	994	995	996	997	998	999	1000
------	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	------

Desafío

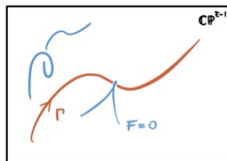
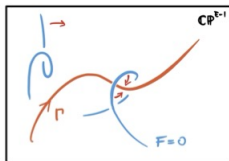
Calcular Δ

7267	222	226	229	230	231	232	233	234	235	236	237	238	239	240	241	242	243	244	245	246	247	248	249	250	251	252	253	254	255	256	257	258	259	260	261	262	263	264	265	266	267	268	269	270	271	272	273	274	275	276	277	278	279	280	281	282	283	284	285	286	287	288	289	290	291	292	293	294	295	296	297	298	299	300	301	302	303	304	305	306	307	308	309	310	311	312	313	314	315	316	317	318	319	320	321	322	323	324	325	326	327	328	329	330	331	332	333	334	335	336	337	338	339	340	341	342	343	344	345	346	347	348	349	350	351	352	353	354	355	356	357	358	359	360	361	362	363	364	365	366	367	368	369	370	371	372	373	374	375	376	377	378	379	380	381	382	383	384	385	386	387	388	389	390	391	392	393	394	395	396	397	398	399	400	401	402	403	404	405	406	407	408	409	410	411	412	413	414	415	416	417	418	419	420	421	422	423	424	425	426	427	428	429	430	431	432	433	434	435	436	437	438	439	440	441	442	443	444	445	446	447	448	449	450	451	452	453	454	455	456	457	458	459	460	461	462	463	464	465	466	467	468	469	470	471	472	473	474	475	476	477	478	479	480	481	482	483	484	485	486	487	488	489	490	491	492	493	494	495	496	497	498	499	500	501	502	503	504	505	506	507	508	509	510	511	512	513	514	515	516	517	518	519	520	521	522	523	524	525	526	527	528	529	530	531	532	533	534	535	536	537	538	539	540	541	542	543	544	545	546	547	548	549	550	551	552	553	554	555	556	557	558	559	560	561	562	563	564	565	566	567	568	569	570	571	572	573	574	575	576	577	578	579	580	581	582	583	584	585	586	587	588	589	590	591	592	593	594	595	596	597	598	599	600	601	602	603	604	605	606	607	608	609	610	611	612	613	614	615	616	617	618	619	620	621	622	623	624	625	626	627	628	629	630	631	632	633	634	635	636	637	638	639	640	641	642	643	644	645	646	647	648	649	650	651	652	653	654	655	656	657	658	659	660	661	662	663	664	665	666	667	668	669	670	671	672	673	674	675	676	677	678	679	680	681	682	683	684	685	686	687	688	689	690	691	692	693	694	695	696	697	698	699	700	701	702	703	704	705	706	707	708	709	710	711	712	713	714	715	716	717	718	719	720	721	722	723	724	725	726	727	728	729	730	731	732	733	734	735	736	737	738	739	740	741	742	743	744	745	746	747	748	749	750	751	752	753	754	755	756	757	758	759	760	761	762	763	764	765	766	767	768	769	770	771	772	773	774	775	776	777	778	779	780	781	782	783	784	785	786	787	788	789	790	791	792	793	794	795	796	797	798	799	800	801	802	803	804	805	806	807	808	809	810	811	812	813	814	815	816	817	818	819	820	821	822	823	824	825	826	827	828	829	830	831	832	833	834	835	836	837	838	839	840	841	842	843	844	845	846	847	848	849	850	851	852	853	854	855	856	857	858	859	860	861	862	863	864	865	866	867	868	869	870	871	872	873	874	875	876	877	878	879	880	881	882	883	884	885	886	887	888	889	890	891	892	893	894	895	896	897	898	899	900	901	902	903	904	905	906	907	908	909	910	911	912	913	914	915	916	917	918	919	920	921	922	923	924	925	926	927	928	929	930	931	932	933	934	935	936	937	938	939	940	941	942	943	944	945	946	947	948	949	950	951	952	953	954	955	956	957	958	959	960	961	962	963	964	965	966	967	968	969	970	971	972	973	974	975	976	977	978	979	980	981	982	983	984	985	986	987	988	989	990	991	992	993	994	995	996	997	998	999	1000
------	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	------

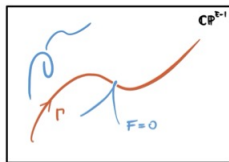
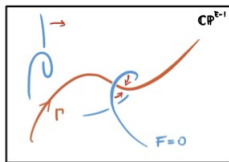
¿Qué monomios/coeficientes tiene?



Importantísimo en aplicaciones



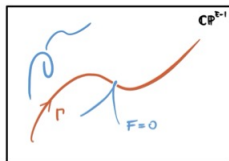
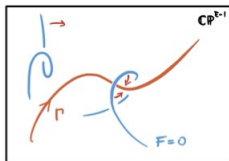
Importantísimo en aplicaciones



■ Física e Ingeniería

- Análisis de estabilidad estructural
- Sistemas oscilatorios

Importantísimo en aplicaciones



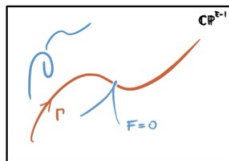
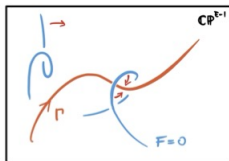
■ Física e Ingeniería

- Análisis de estabilidad estructural
- Sistemas oscilatorios

■ Economía y Finanzas

- Problemas de optimización
- Estrategias de equilibrio

Importantísimo en aplicaciones



■ Física e Ingeniería

- Análisis de estabilidad estructural
- Sistemas oscilatorios

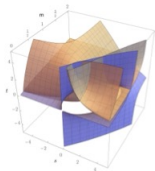
■ Economía y Finanzas

- Problemas de optimización
- Estrategias de equilibrio

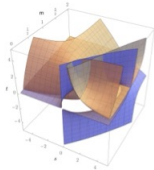
■ Diseño gráfico computacional

- gráficos dinámicos de curvas y superficies
- cálculos de intersecciones

Más aplicaciones

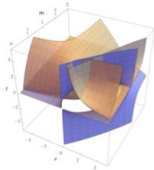


Más aplicaciones



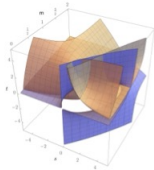
- **Análisis de sistemas de información geográfica**
 - Modelado de accidentes geográficos
 - Predicción de trayectorias

Más aplicaciones



- **Análisis de sistemas de información geográfica**
 - Modelado de accidentes geográficos
 - Predicción de trayectorias
- **Investigación en medicina y farmacología**
 - Regulación/combinación de dosis
 - Modelado de procesos biológicos

Más aplicaciones



- **Análisis de sistemas de información geográfica**
 - Modelado de accidentes geográficos
 - Predicción de trayectorias
- **Investigación en medicina y farmacología**
 - Regulación/combinación de dosis
 - Modelado de procesos biológicos
- . . .

Discriminantes y Alicia Dickenstein

Discriminantes y Alicia Dickenstein

- MR4599256** Reviewed Dickenstein, Alicia; Di Rocco, Sandra; Morrison, Ralph Iterated and mixed discriminants. *J. Comb. Algebra* 7 (2023), no. 1-2, 45–81. (Reviewer: Haohao Wang) 13P15 (14Q20 52A39 52B20) 
[Review PDF](#) | [Clipboard](#) | [Journal](#) | [Article](#)

- MR3289657** Reviewed Dickenstein, Alicia; Emiris, Ioannis Z.; Karasoulou, Anna Plane mixed discriminants and toric Jacobians. *SAGA—Advances in ShApes, Geometry, and Algebra*, 105–121, *Geom. Comput.*, 10, Springer, Cham, 2014. (Reviewer: Hossein Sabzrou) 13P15
[Review PDF](#) | [Clipboard](#) | [Series](#) | [Chapter](#) | [5 Citations](#) 

- MR3078246** Reviewed Cattani, Eduardo; Cueto, María Angélica; Dickenstein, Alicia; Di Rocco, Sandra; Sturmfels, Bernd Mixed discriminants. *Math. Z.* 274 (2013), no. 3-4, 761–778. (Reviewer: Maria-Laura Torrente) 14M12 (13P15 14M25 14T05 52B40) 
[Review PDF](#) | [Clipboard](#) | [Journal](#) | [Article](#) | [20 Citations](#)

- MR2911928** Reviewed Dickenstein, Alicia; Nill, Benjamin; Vergne, Michèle A relation between number of integral points, volumes of faces and degree of the discriminant of smooth lattice polytopes. *C. R. Math. Acad. Sci. Paris* 350 (2012), no. 5-6, 229–233. (Reviewer: Matthias Beck) 52B20 (11H06 11P21 14M25) 
[Review PDF](#) | [Clipboard](#) | [Journal](#) | [Article](#) | [1 Citation](#)

- MR2500350** Reviewed Cueto, María Angélica; Dickenstein, Alicia Some results on inhomogeneous discriminants. *Proceedings of the XVth Latin American Algebra Colloquium (Spanish)*, 41–62, *Bibl. Rev. Mat. Iberoamericana, Rev. Mat. Iberoamericana, Madrid*, 2007. (Reviewer: Luis David García-Puente) 14M25 (13P05 14E05 68W30) 
[Review PDF](#) | [Clipboard](#) | [Series](#) | [Chapter](#) | [8 Citations](#)

- MR2343141** Reviewed Dickenstein, Alicia; Rojas, J. Maurice; Rusek, Korben; Shih, Justin Extremal real algebraic geometry and \mathcal{A} -discriminants. *Mosc. Math. J.* 7 (2007), no. 3, 425–452, 574. (Reviewer: Meirav Topol-Amram) 14M25 (14P25 34C08) 
[Review PDF](#) | [Clipboard](#) | [Journal](#) | [Article](#) | [12 Citations](#)

- MR2328718** Reviewed Dickenstein, Alicia; Feichtner, Eva Maria; Sturmfels, Bernd Tropical discriminants. *J. Amer. Math. Soc.* 20 (2007), no. 4, 1111–1133. (Reviewer: G. K. Sankaran) 14M25 (52B20) 
[Review PDF](#) | [Clipboard](#) | [Journal](#) | [Article](#) | [70 Citations](#)

Cueto, María Angélica; Dickenstein, Alicia
Some results on inhomogeneous discriminants
Rev. Mat. Iberoamericana, 2007

Cueto, María Angélica; Dickenstein, Alicia
Some results on inhomogeneous discriminants
Rev. Mat. Iberoamericana, 2007

- Muestran la biracionalidad de la parametrización de Horn-Kapranov de Δ

Cueto, María Angélica; Dickenstein, Alicia
Some results on inhomogeneous discriminants
Rev. Mat. Iberoamericana, 2007

- Muestran la biracionalidad de la parametrización de Horn-Kapranov de Δ
- Varias “recetas” para simplificar el cálculo de Δ

Cueto, María Angélica; Dickenstein, Alicia
Some results on inhomogeneous discriminants
Rev. Mat. Iberoamericana, 2007

- Muestran la biracionalidad de la parametrización de Horn-Kapranov de Δ
- Varias “recetas” para simplificar el cálculo de Δ
- Estudio de Δ en codimensión 3

Otra aplicación de Horn-Kapranov

Dickenstein, Alicia; Rojas, J. Maurice; Rusek,
Korben; Shih, Justin

**Extremal real algebraic geometry and
 \mathcal{A} -discriminants**

Mosc. Math. J. 7 (2007)

Otra aplicación de Horn-Kapranov

Dickenstein, Alicia; Rojas, J. Maurice; Rusek,
Korben; Shih, Justin

**Extremal real algebraic geometry and
 \mathcal{A} -discriminants**

Mosc. Math. J. 7 (2007)

Contraejemplos simples de la conjetura de
Kushnirenko

Conjetura de Kushnirenko (1970)

Conjetura de Kushnirenko (1970)

el número de soluciones aisladas
positivas de

$$\begin{cases} a_1 x^{\alpha_1} y^{\beta_1} + a_2 x^{\alpha_2} y^{\beta_2} + a_3 x^{\alpha_3} y^{\beta_3} = 0 \\ b_1 x^{\alpha'_1} y^{\beta'_1} + b_2 x^{\alpha'_2} y^{\beta'_2} + b_3 x^{\alpha'_3} y^{\beta'_3} = 0 \end{cases}$$

es a lo sumo 4

$$\forall a_1, b_1, a_2, b_2, a_3, b_3 \in \mathbb{R}$$

$$\forall \alpha_1, \alpha'_1, \dots, \beta_3, \beta'_3 \in \mathbb{N}$$

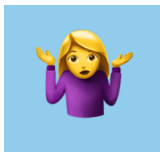


Contraejemplo de Haas (2000)

Contraejemplo de Haas (2000)

$$\begin{cases} x^{106} + 1.1y^{53} - 1.1y = 0 \\ y^{106} + 1.1x^{53} - 1.1x = 0 \end{cases}$$

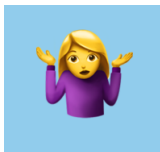
tiene **5** raíces positivas aisladas



Contraejemplo de Haas (2000)

$$\begin{cases} x^{106} + 1.1y^{53} - 1.1y = 0 \\ y^{106} + 1.1x^{53} - 1.1x = 0 \end{cases}$$

tiene 5 raíces positivas aisladas



Li-Rojas-Wang 03: la cota es 5

DRRS 07

DRRS 07

$$\begin{cases} x^6 + \frac{44}{31}y^3 - y = 0 \\ y^6 + \frac{44}{31}x^3 - x = 0 \end{cases}$$

también tiene 5 raíces positivas

DRRS 07

$$\begin{cases} x^6 + \frac{44}{31}y^3 - y = 0 \\ y^6 + \frac{44}{31}x^3 - x = 0 \end{cases}$$

también tiene 5 raíces positivas
La probabilidad de encontrar estos
contraejemplos es MUY baja

Volvemos al MateMax!

Torneo eliminatorio



64 jugadoras van a competir en un torneo de tenis. En cada partido, la jugadora que pierda quedará eliminada, pero le regalarán un par de zapatillas marca "Gabriela Corazón". La que gane un partido, volverá a jugar contra otra rival, hasta que se determine la ganadora del torneo.

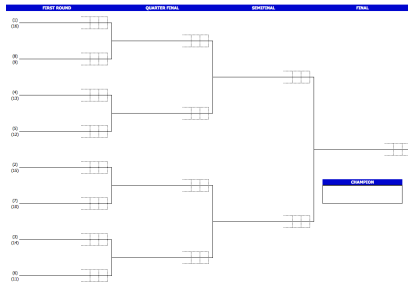
¿Cuántos pares de zapatillas van a regalar?

¿Cuántos partidos van a jugarse en total para hallar la ganadora?

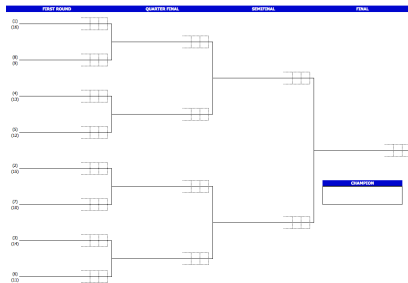


Solución

Solución

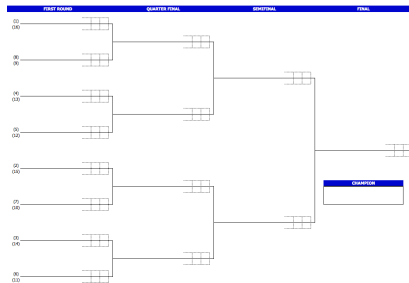


Solución



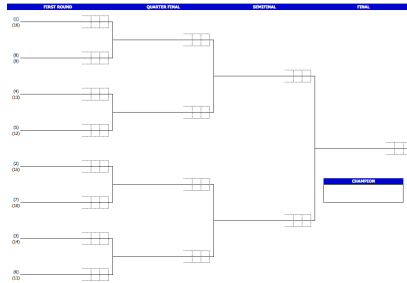
32

Solución



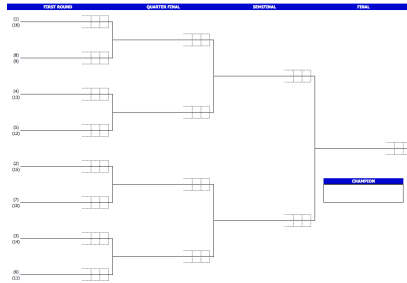
$$32 + 16$$

Solución



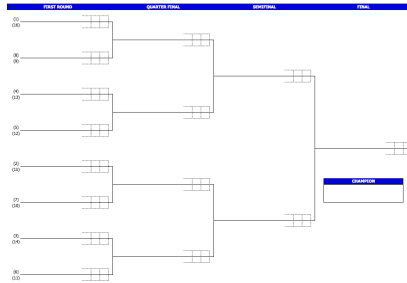
$$32 + 16 + 8$$

Solución



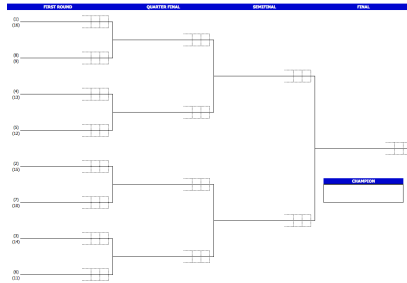
$$32 + 16 + 8 + 4$$

Solución



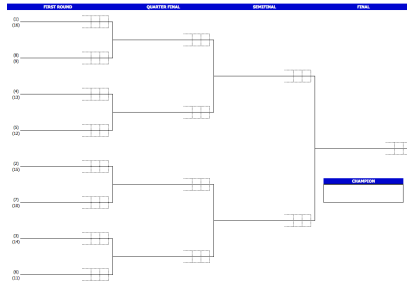
$$32 + 16 + 8 + 4 + 2$$

Solución



$$32 + 16 + 8 + 4 + 2 + 1$$

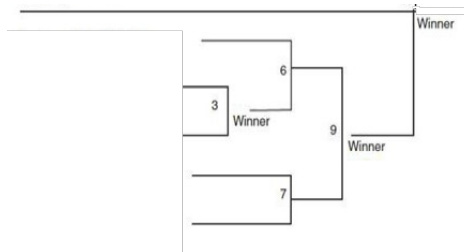
Solución



$$32 + 16 + 8 + 4 + 2 + 1 = \boxed{63}$$

El problema no aclara el fixture!

El problema no aclara el fixture!



A ver....



A ver....



- En cada partido se elimina **1** chica

A ver....

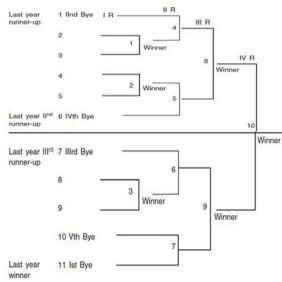


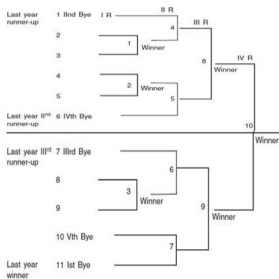
- En cada partido se elimina **1** chica
- Al final del torneo habrán

A ver....



- En cada partido se elimina **1** chica
- Al final del torneo habrán
 $64 - 1 = 63$ eliminadas





Teorema

En un torneo cualquiera con N jugadoras a simple eliminación, habrán de jugarse $N - 1$ partidos

Final de la pausa!

Final de la pausa!

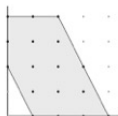
Dickenstein, Alicia; Feichtner, Eva; Sturmfels, Bernd
Tropical discriminants.
J. Amer. Math. Soc. 20 (2007)

Final de la pausa!

Dickenstein, Alicia; Feichtner, Eva; Sturmfels, Bernd

Tropical discriminants.

J. Amer. Math. Soc. 20 (2007)



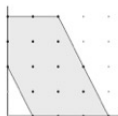
- Tropicalización de la parametrización de Horn-Kapranov

Final de la pausa!

Dickenstein, Alicia; Feichtner, Eva; Sturmfels, Bernd

Tropical discriminants.

J. Amer. Math. Soc. 20 (2007)



- Tropicalización de la parametrización de Horn-Kapranov
- Cálculo de $N(\Delta)$

Matemática discreta y convexidad

Dickenstein, Alicia; Nill, Benjamin; Vergne, Michèle
**A relation between number of integral points,
volumes of faces and degree of the
discriminant of smooth lattice polytopes**
C. R. Math. Acad. Sci. Paris 350 (2012)

Matemática discreta y convexidad

Dickenstein, Alicia; Nill, Benjamin; Vergne, Michèle

**A relation between number of integral points,
volumes of faces and degree of the
discriminant of smooth lattice polytopes**

C. R. Math. Acad. Sci. Paris 350 (2012)

$\deg(\Delta(F))$ depende de volúmenes de
caras de $N(F)$

Matemática discreta y convexidad

Dickenstein, Alicia; Nill, Benjamin; Vergne, Michèle
**A relation between number of integral points,
volumes of faces and degree of the
discriminant of smooth lattice polytopes**

C. R. Math. Acad. Sci. Paris 350 (2012)

$\deg(\Delta(F))$ depende de volúmenes de
caras de $N(F)$

Se calcula $\deg(\Delta(F))$ en función del
 $\#$ puntos enteros en $\lambda N(F)^\circ$



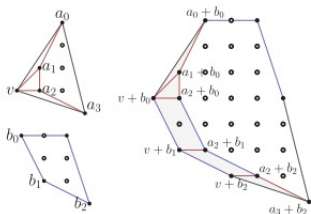
Cattani, Eduardo; Cueto, María Angélica;
Dickenstein, Alicia; Di Rocco, Sandra; Sturmfels,
Bernd

Mixed discriminants

Math. Z. 274 (2013)

Cattani, Eduardo; Cueto, María Angélica;
 Dickenstein, Alicia; Di Rocco, Sandra; Sturmfels,
 Bernd

Mixed discriminants
 Math. Z. 274 (2013)



$$\deg_j(\Delta(F_1, F_2)) = a(N_1 + N_2) - a(N_i) - p(N_j)$$

Dickenstein, Alicia; Di Rocco, Sandra; Morrison,
Ralph

Iterated and mixed discriminants

J. Comb. Algebra 7 (2023)

Dickenstein, Alicia; Di Rocco, Sandra; Morrison,
Ralph

Iterated and mixed discriminants

J. Comb. Algebra 7 (2023)

$$F = a + bx + cy + dx^2 + ey^2 + fxy$$
$$\Delta = -4adf + ae^2 + b^2f - bce + c^2d$$

Dickenstein, Alicia; Di Rocco, Sandra; Morrison,
Ralph

Iterated and mixed discriminants

J. Comb. Algebra 7 (2023)

$$F = a + bx + cy + dx^2 + ey^2 + fxy$$

$$\Delta = -4adf + ae^2 + b^2f - bce + c^2d$$

$$\Delta_x(F) =$$

$$\Delta_x((a + cy + fy^2) + (b + fy)x + dx^2)$$

Dickenstein, Alicia; Di Rocco, Sandra; Morrison,
Ralph

Iterated and mixed discriminants

J. Comb. Algebra 7 (2023)

$$F = a + bx + cy + dx^2 + ey^2 + fxy$$

$$\Delta = -4adf + ae^2 + b^2f - bce + c^2d$$

$$\Delta_x(F) =$$

$$\Delta_x((a + cy + fy^2) + (b + fy)x + dx^2) =$$
$$(b + fy)^2 - 4d(a + cy + fy^2)$$

Dickenstein, Alicia; Di Rocco, Sandra; Morrison,
Ralph

Iterated and mixed discriminants

J. Comb. Algebra 7 (2023)

$$F = a + bx + cy + dx^2 + ey^2 + fxy$$

$$\Delta = -4adf + ae^2 + b^2f - bce + c^2d$$

$$\Delta_x(F) =$$

$$\Delta_x((a + cy + fy^2) + (b + fy)x + dx^2) =$$
$$(b + fy)^2 - 4d(a + cy + fy^2)$$

$$\Delta_y(\Delta_x(F)) = 16d\Delta$$

Para saber más....

Para saber más....

MATEMAX

Computational Algebra, Algebraic Geometry and Applications II

Buenos Aires, Argentina, December 15-17 2025



Celebrating Alicia Dickenstein's contributions to Math and beyond

SAVE THE DATE!

<http://mate.dm.uba.ar/~coalaga/>



Epílogo-Max



Epílogo-Max



Hay tres cosas que cada persona debería hacer durante su vida:

Epílogo-Max



Hay tres cosas que cada persona debería hacer durante su vida:

- Plantar un árbol

Epílogo-Max



Hay tres cosas que cada persona debería hacer durante su vida:

- Plantar un árbol
- Tener un hijo

Epílogo-Max

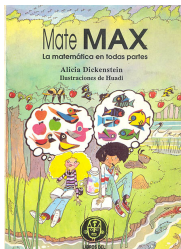


Hay tres cosas que cada persona debería hacer durante su vida:

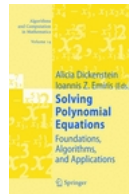
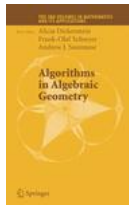
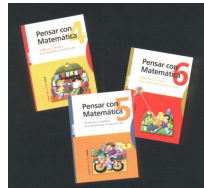
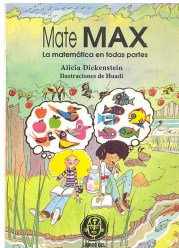
- Plantar un árbol
- Tener un hijo
- Escribir un libro

Escribir un libro

Escribir un libro



Escribir un libro



Tener un hijo

Tener un hijo

Mathematics Genealogy Project

Alicia Dickenstein

[MathSciNet](#)

Ph.D. [Universidad de Buenos Aires](#) 1982



Dissertation: *Cohomología moderada con soporte en intersecciones no completas*

Mathematics Subject Classification: 54—General topology

Advisor 1: [Miguel E. M. Herrera](#)

Students:

Click [here](#) to see the students listed in chronological order.

Name	School	Year	Descendants
Botbol, Nicolás	Institut de Mathématiques de Jussieu and Universidad de Buenos Aires	2010	
D'Andrea, Carlos	Universidad de Buenos Aires	2001	2
Giaroli, Magalí	Universidad de Buenos Aires	2019	
Martínez, Federico	Universidad de Buenos Aires	2011	
Pérez Millán, Mercedes	Universidad de Buenos Aires	2012	
Tobis, Enrique	Universidad de Buenos Aires	2009	



Plantar un árbol?



Plantar un árbol?



MATEMAX

Computational Algebra, Algebraic Geometry and Applications II

Buenos Aires, Argentina, December 15-17 2025



Celebrating Alicia Dickenstein's contributions to Math and beyond

SAVE THE DATE!

<http://mate.dm.uba.ar/~coalaga/>